

# Eco-efficient aircraft trajectories

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Wissen für Morgen



# FlyATM4E (SESAR ER)

## Mitigating aviation climate impact by climate-optimized aircraft trajectories

SESAR Exploratory Research Project, *Grant No 891317*

### Sigrun Matthes

Florian Linke, Feijia Yin, Manuel Soler, Benjamin Lührs, Simone Dietmüller, Patrick Peter et al.

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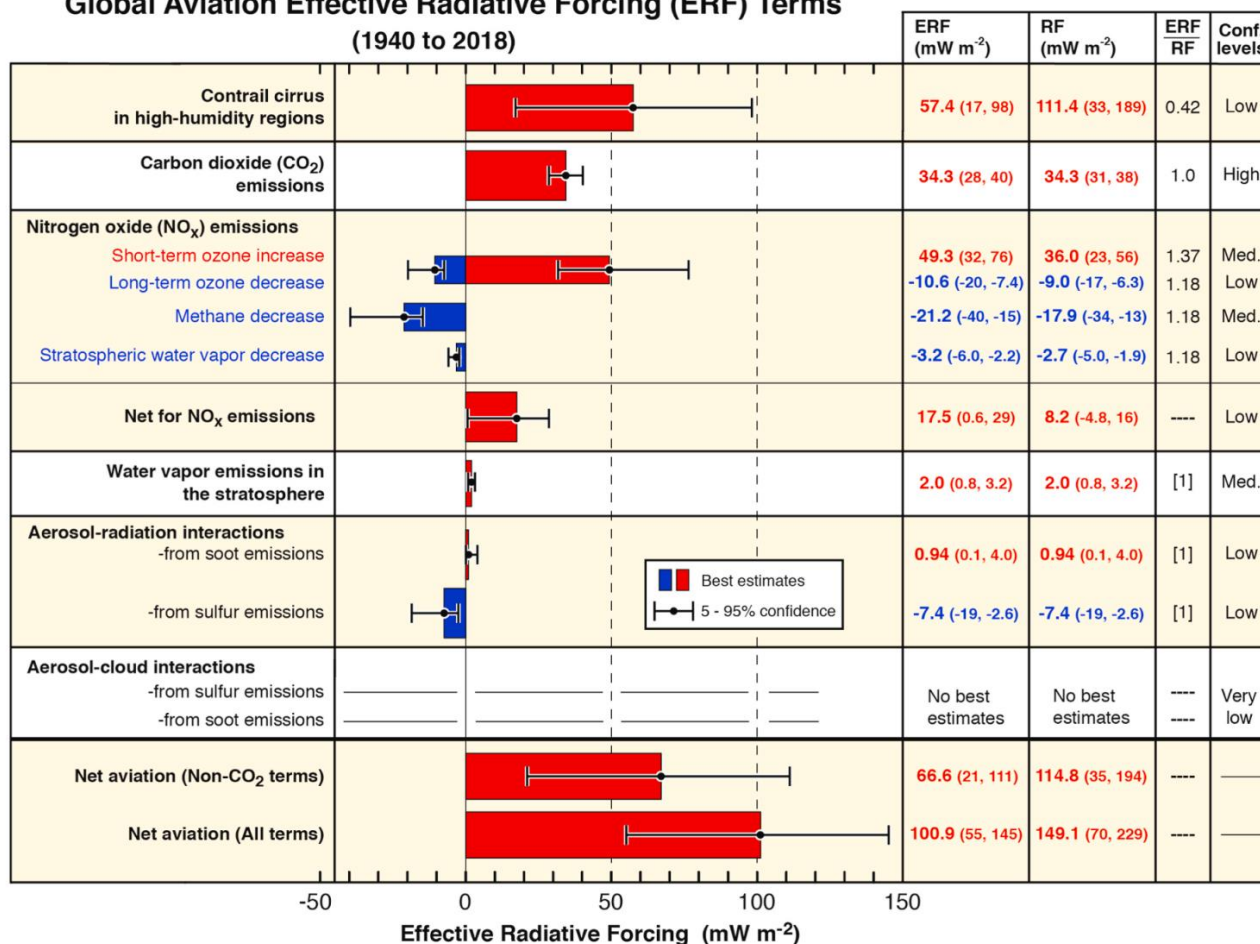


Wissen für Morgen



# Effective radiative forcing (ERF)

Global Aviation Effective Radiative Forcing (ERF) Terms (1940 to 2018)



Lee et al., 2021

$$\Delta T = \lambda \text{ ERF}$$

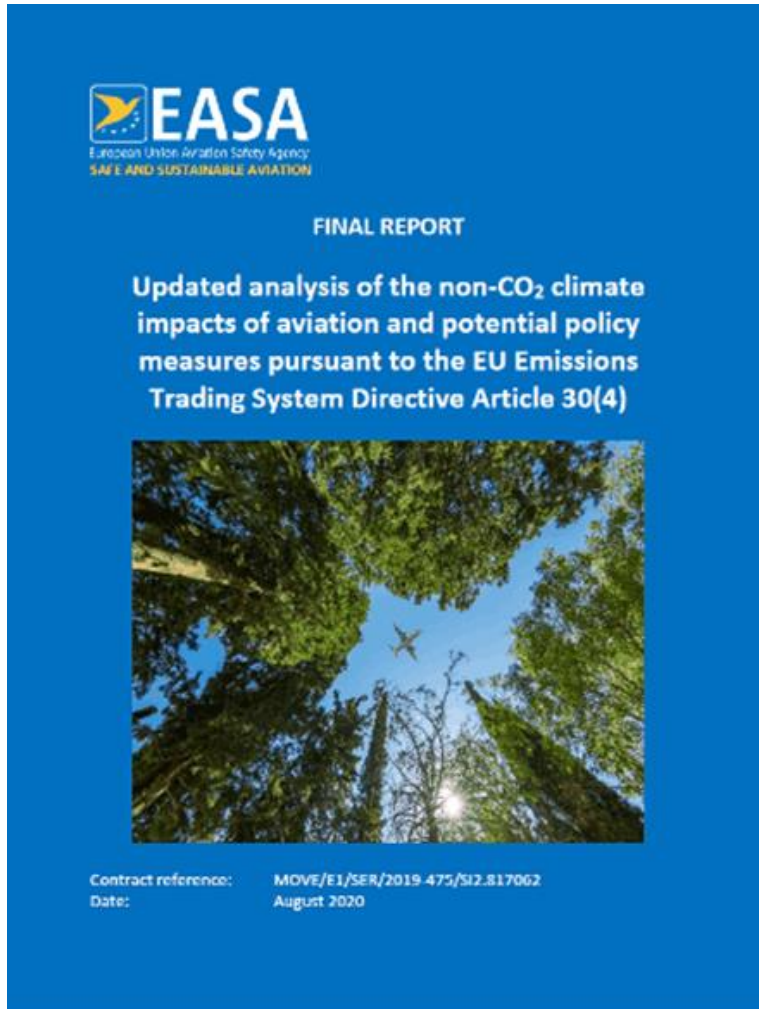
➤ According to Lee et al. (2021) non-CO<sub>2</sub> effects contribute at least 2/3 to the total aviation ERF.

➤ Non-CO<sub>2</sub> effects also occur if alternative fuels are used, in particular H<sub>2</sub>; changes are expected.

➤ The magnitude of the non-CO<sub>2</sub> effects depends on location and time of the emissions.



# Non-CO<sub>2</sub> effects of aviation: Concepts in Europe



**EASA**  
European Union Aviation Safety Agency  
SAFE AND SUSTAINABLE AVIATION

FINAL REPORT

Updated analysis of the non-CO<sub>2</sub> climate impacts of aviation and potential policy measures pursuant to the EU Emissions Trading System Directive Article 30(4)

Contract reference: MOVE/E1/SER/2019-475/SI2.817062  
Date: August 2020

Type of Measure		Main non-CO <sub>2</sub> effect(s) addressed by the measure
Financial	1. NO <sub>x</sub> charge	NO <sub>x</sub>
	2. Inclusion of aircraft NO <sub>x</sub> emissions in EU ETS	NO <sub>x</sub>
Fuel	3. Reduction in maximum limit of aromatics within fuel specifications	Soot particulates and contrail-cirrus
	4. Mandatory use of Sustainable Aviation Fuels (SAF)	Soot particulates and contrail-cirrus
ATM	5. Avoidance of ice-supersaturated areas	Contrail-cirrus
	6. A climate charge	All (NO <sub>x</sub> , water vapour, soot, sulphates, contrails)

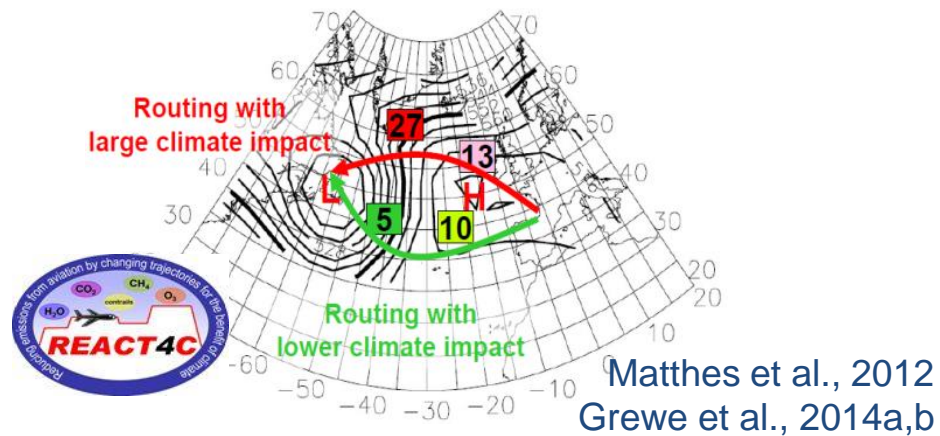
*Arrowsmith et al., 2020*



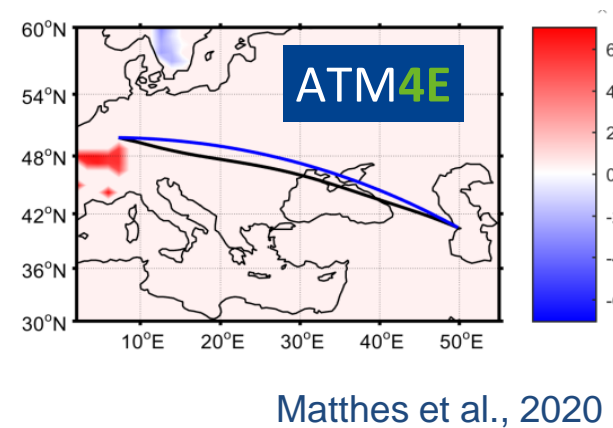
# FlyATM4E Climate-optimization of aircraft trajectories

- Aviation is concerned by reducing climate impact of its operations. **Aviation climate impact** is caused by CO<sub>2</sub> and non-CO<sub>2</sub> emissions, comprising impacts of **contrails**, **nitrogen oxides** impacting ozone and methane, **water vapour**, and **aerosol effects**.
- Non-CO<sub>2</sub> climate impacts** show a strong spatial and temporal variation, which can be exploited when identifying **alternative trajectories**, by **avoiding those regions** where emissions have a large impact.
- However, during flight planning currently emission information is available, but no **environmental impact information** linked to the emitted amount is available along the trajectory.

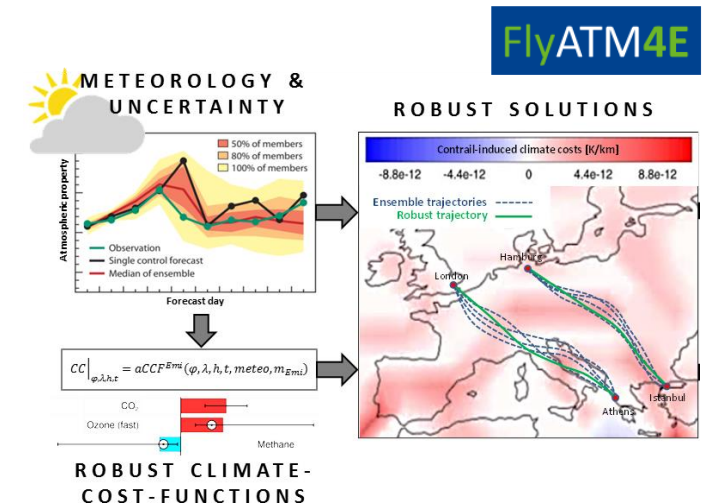
## Concept: Feasibility study



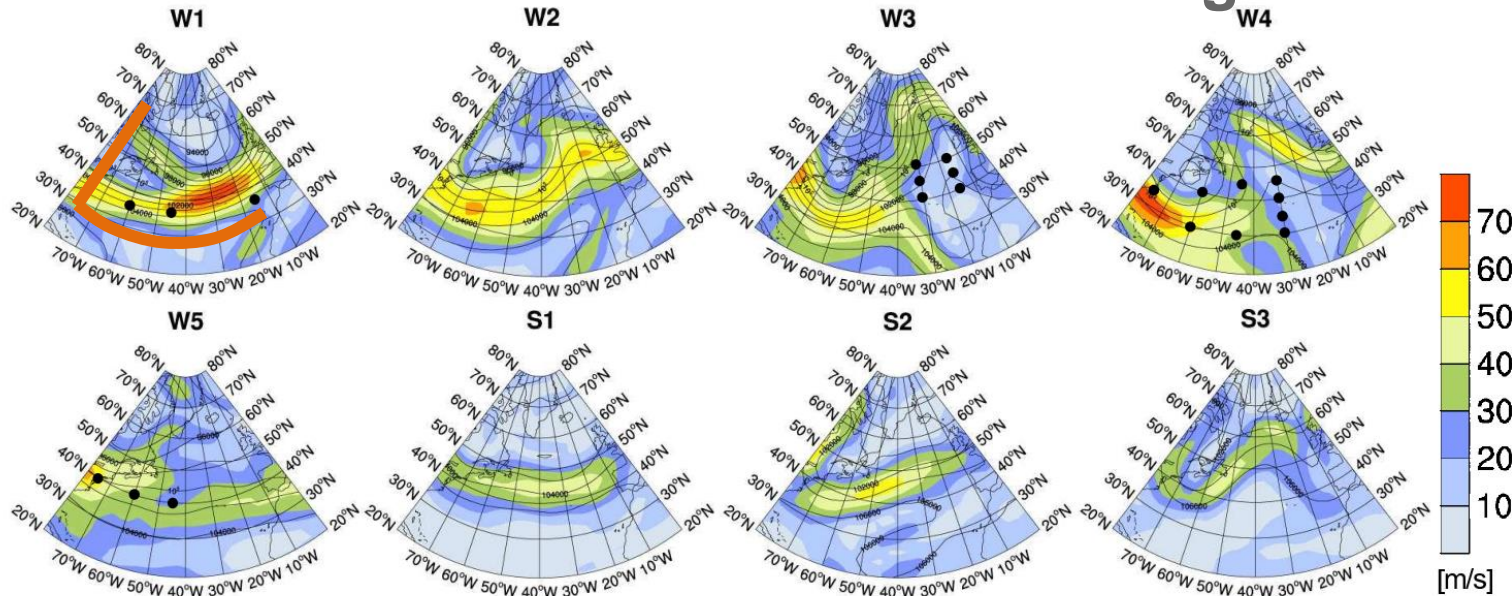
## European Application: Case study



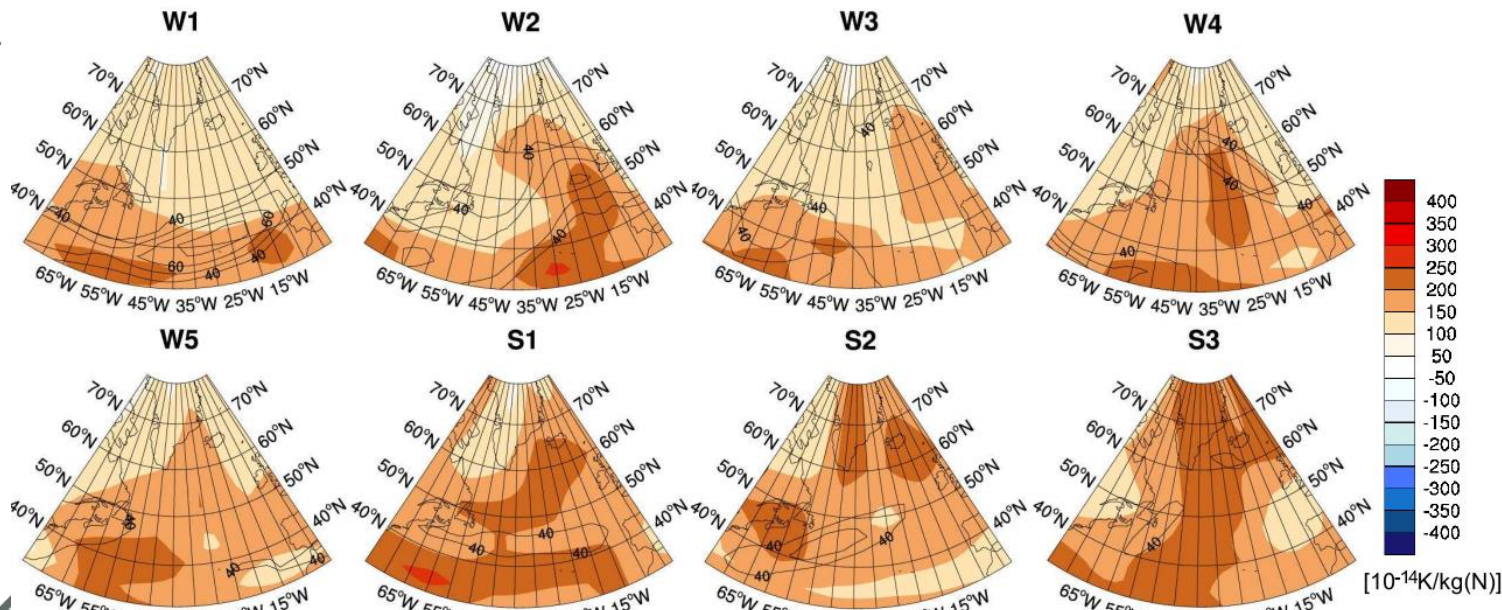
## Uncertainties and robustness



# Weather data and Ozone Climate-Change-Functions



**Climatology of aviation weather situations:**  
 Winter W1-W5  
 Summer S1-S3  
 University Reading  
 Irvine et al. 2013



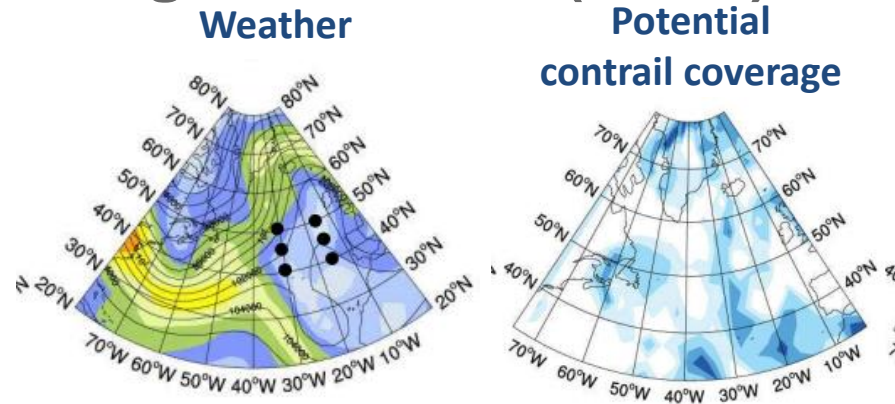
**Contribution of a local NO<sub>x</sub> emission to climate change via ozone formation**

**Clear relationship between weather and CCFs**

Frömming et al. 2021

# MET Service: Climate Change Functions (CCFs)

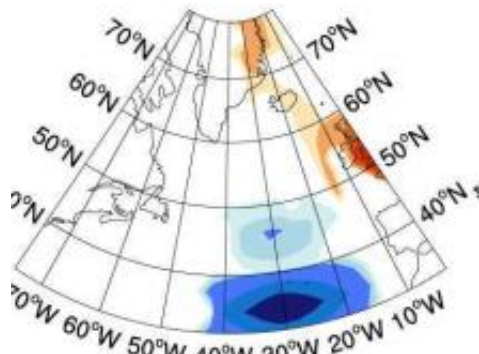
representative winter  
weather situation,  
250 hPa



Frömming et al. 2021

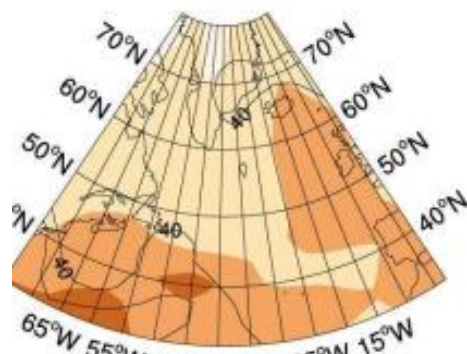
**Climate Change Functions = four dimensional functions (space & time)**

**Contrail CCF**



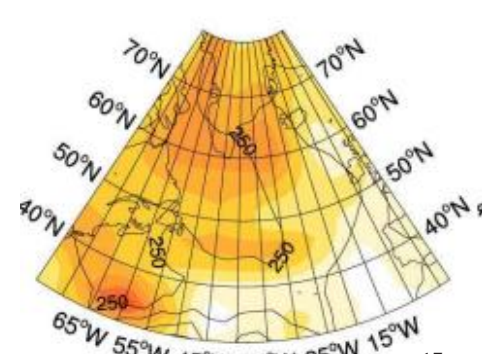
$[10^{-14} \text{K/km(contrail)}]$

**Ozone CCF**



$[10^{-14} \text{K/kg(N)}]$

**Water vapour CCF**



$[10^{-17} \text{K/kg(fuel)}]$

- Climate change functions characterize sensitivity of the atmosphere to aviation emissions at specific location (position, altitude, time).  $\Rightarrow$  **MET products for climate-optimized trajectory planning** require spatially and temporally resolved climate impact information.

# Climate impact mitigation potentials of alternative routings

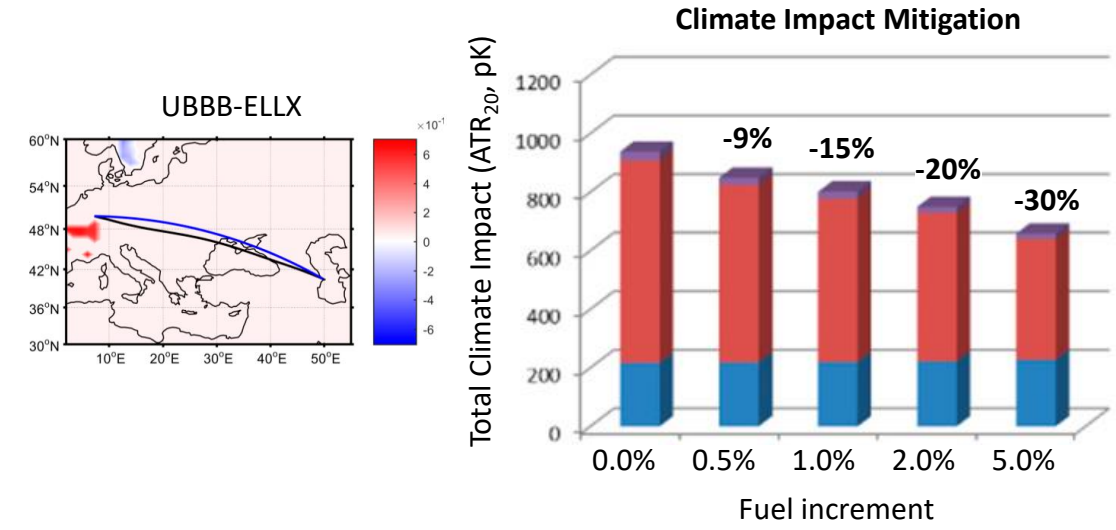
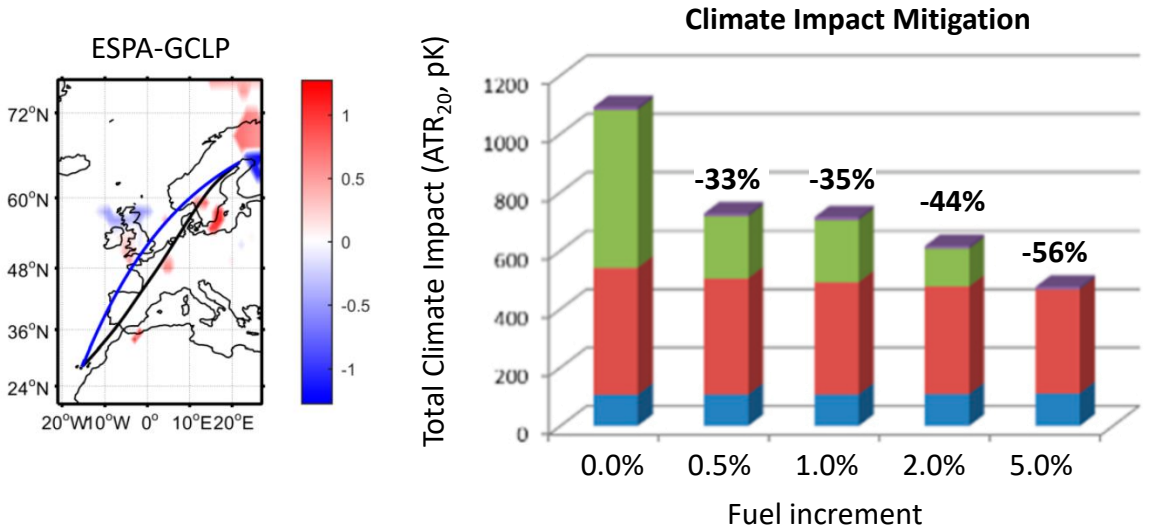


One Day Case Study of European Air Traffic on 18 December 2015

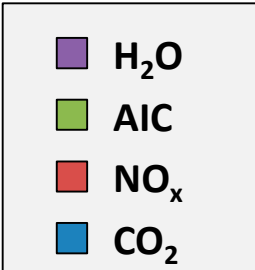
[Matthes et al., 2020](#)

**Example 1: Lulea – Gran Canaria (ESPA-GCLP)**  
**Contrails-dominated climate impact**

**Example 2: Baku – Luxembourg (UBBB-ELLX)**  
**NO<sub>x</sub>-dominated climate impact (no contrails)**



- Climate-optimized routings can mitigate the total climate impact significantly
- The total climate impact of a flight can decrease despite increasing emissions (e.g. -35% ATR<sub>20</sub> for +1% fuel increase)
- Climate-optimized routings might not be cost-optimal (need for market-based / policy measures)



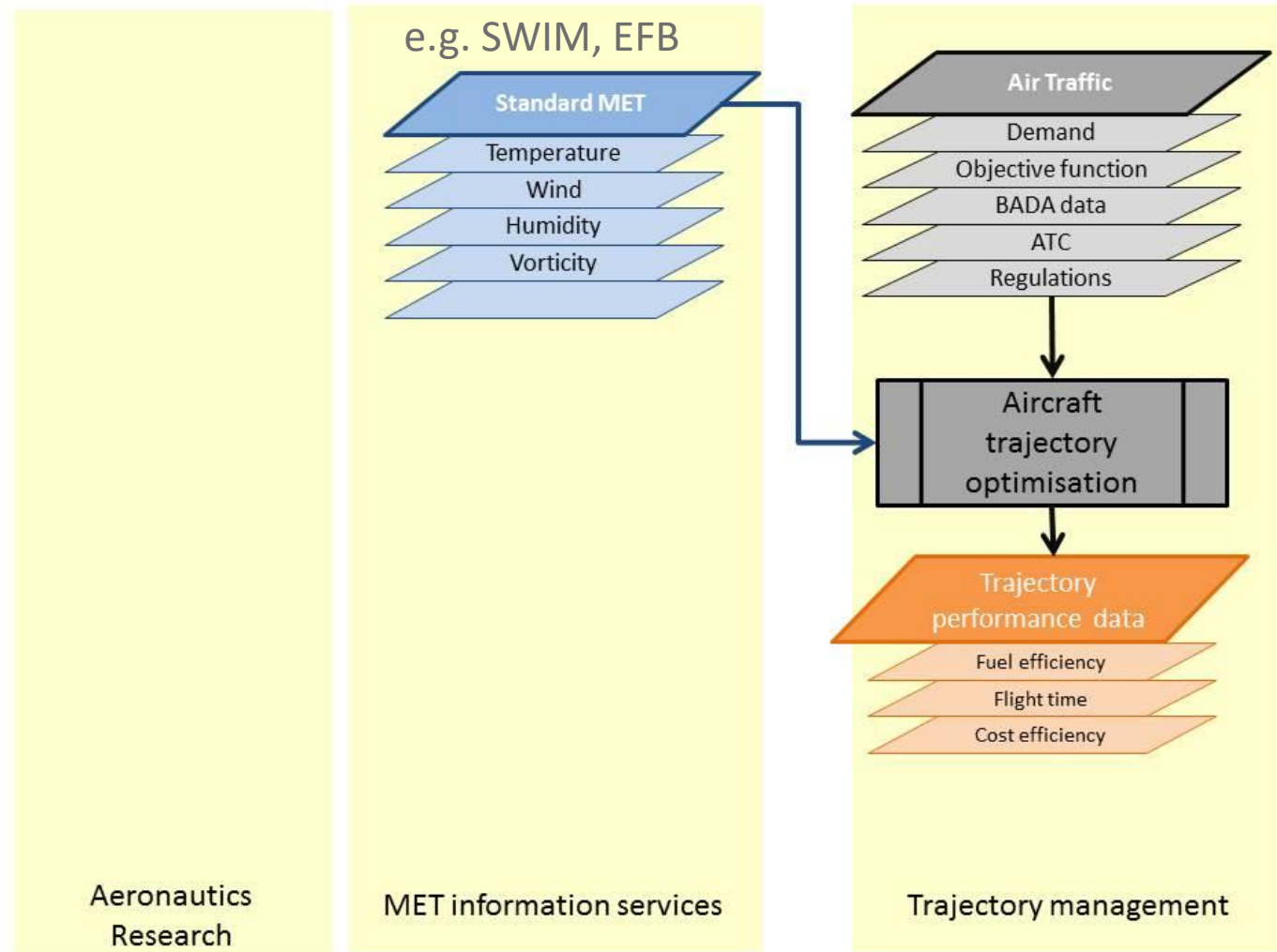
This project has received funding from the SESAR Joint Undertaking under grant agreements No 699395 and No 891317 under European Union's Horizon 2020 research and innovation programme.



# Air traffic management for environment

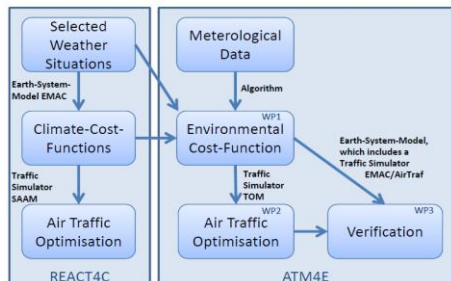
## How to integrate climate change information (aCCFs) during flight planning

### Schematic ATM system

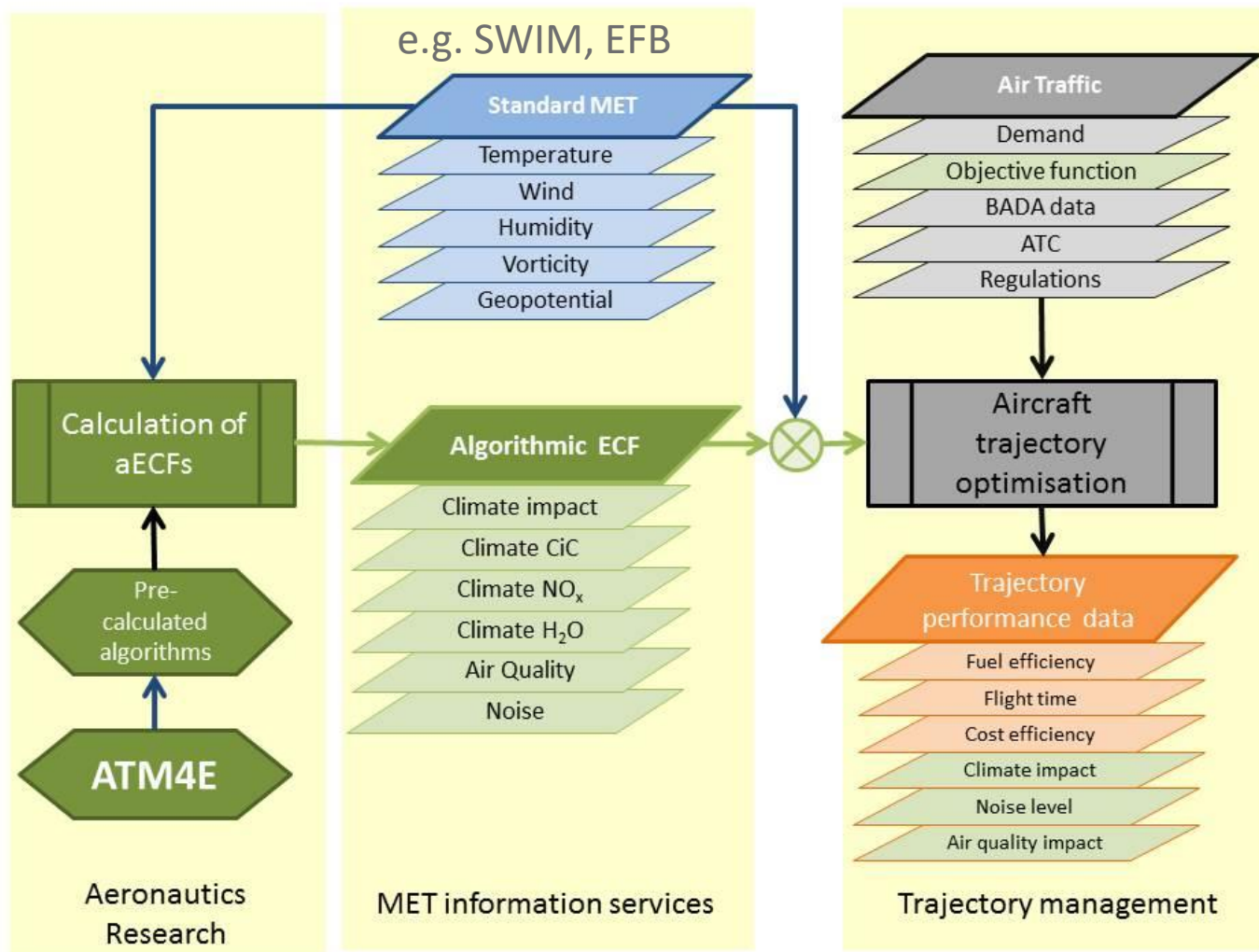


# Air traffic management for environment

## How to integrate climate change information (aCCFs) during flight planning



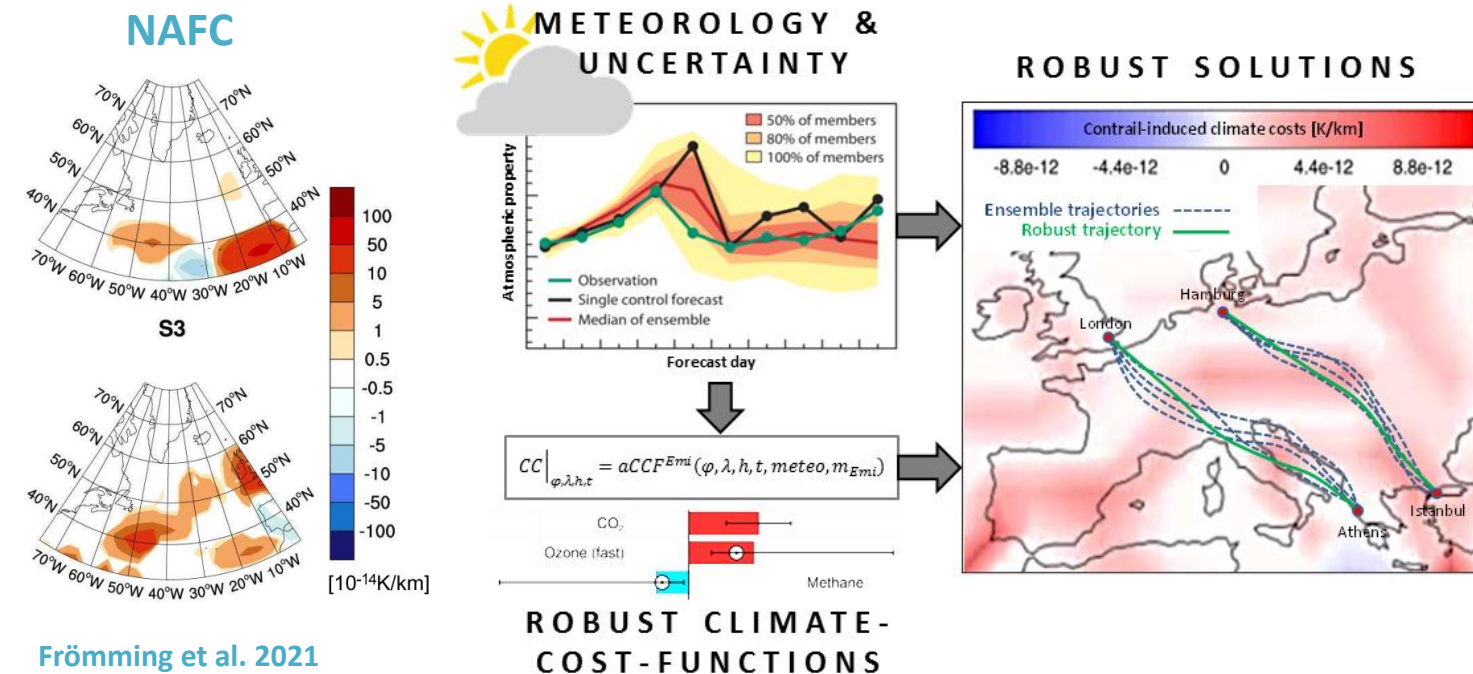
### Contribution of ATM4E



# Feasibility study: Step towards robustness of climate-optimized trajectories

## Using algorithmic Climate Change Functions ECFs (MET service)

- FlyATM4E developed a concept to **identify climate-optimised aircraft trajectories** which enables a robust and **eco-efficient** reduction in aviation’s climate impact, quantifying non-CO<sub>2</sub> **mitigation potentials**.
- FlyATM4E **identified those weather situations** and aircraft trajectories, which lead to a **robust climate impact reduction** despite **uncertainties**. Methods on robust decision making under uncertainty conditions are currently under development, resulting in quantitative estimates of robust mitigation potentials.



- FlyATM4E further identified those weather situations having a **large potential to reduce the climate impact** with only little or even no cost changes (“**Cherry-Picking**”) and those situations where both, climate impact and costs can be reduced (“**Win-Win**”).
- FlyATM4E **formulates recommendations** how to implement these **strategies in meteorological (MET) products**

# Characterization of prevailing uncertainties when providing climate change functions (CCFs)

Prevailing uncertainties need to be characterized and **mathematical concepts** for a risk assessment on how to integrate identified uncertainties in the overall climate effects assessment need to be introduced.

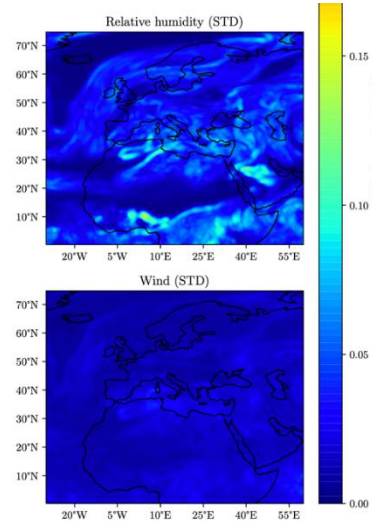
This is a prerequisite in order to **characterize robustness** of alternative **climate-optimized aircraft** trajectories and associated mitigation gains.

## Quality of the meteorological forecast

### Ensemble Prediction System (EPS)



Statistical analysis of key parameters in individual ensemble members, e.g. humidity, temperature, wind.



Simorgh et al. 2022  
Dietmüller et al., 2022

## Representation atmospheric processes

## Physical climate metrics

## Development aCCFs



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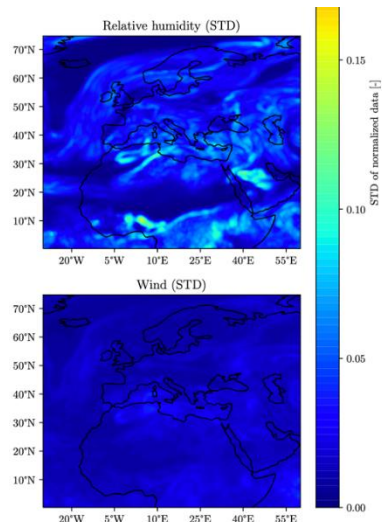
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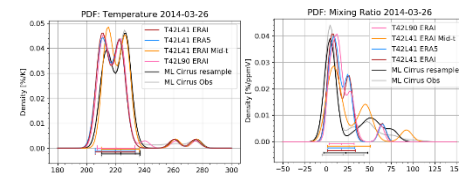
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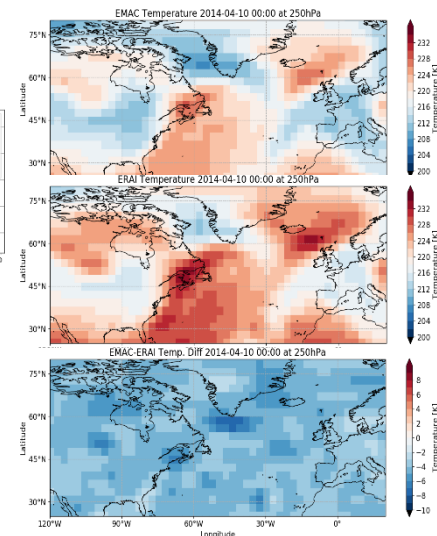
## Representation atmospheric processes

### Nudged simulations in chemistry-climate model EMAC



Temperature Water vapour

Systematic evaluation of chemistry-climate model EMAC with reanalysis and observation data to determine uncertainty.



Peter et al. 2022

## Physical climate metrics

## Development aCCFs



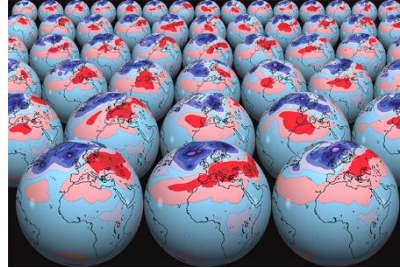
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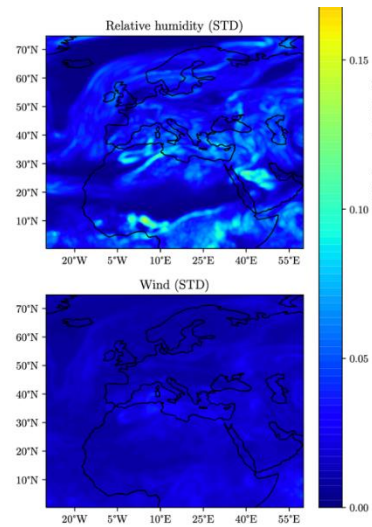
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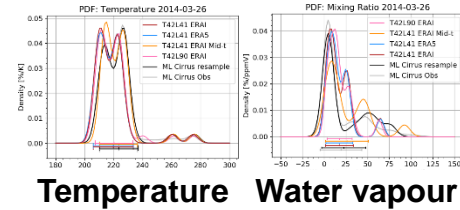
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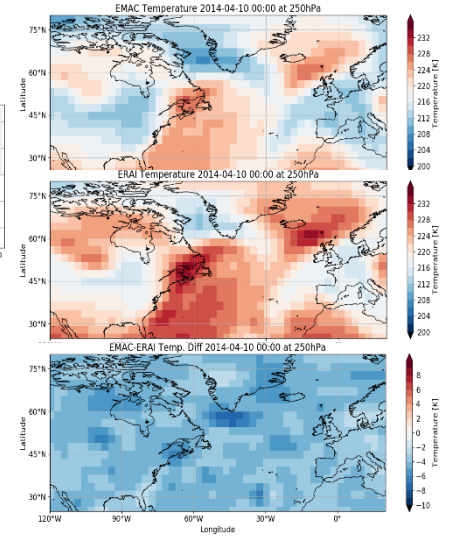
Simorg et al. 2022  
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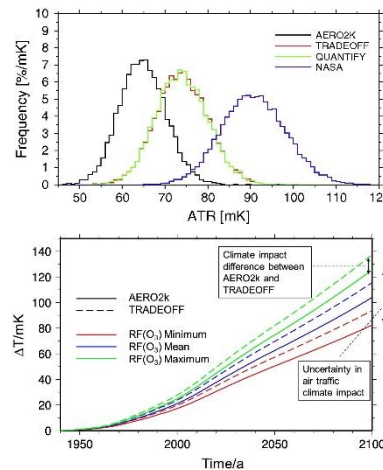


Peter et al. 2022

## Physical climate metrics

Climate metrics are calculated with climate response model AirClim

Calculation of temperature change of CO<sub>2</sub> and non-CO<sub>2</sub> effects requires a physical metric definition, as well as assumptions on background conditions, resulting in uncertainty ranges identified by Monte Carlo simulations.



Dahlmann et al. 2016

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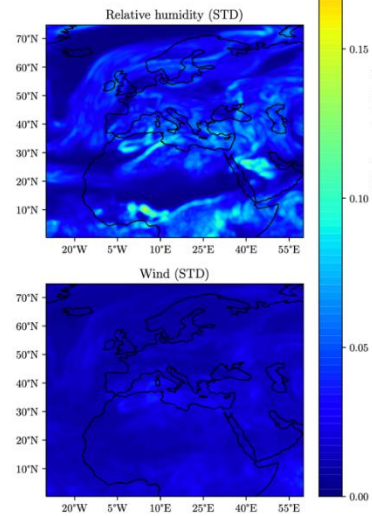
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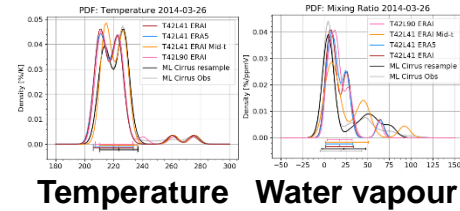
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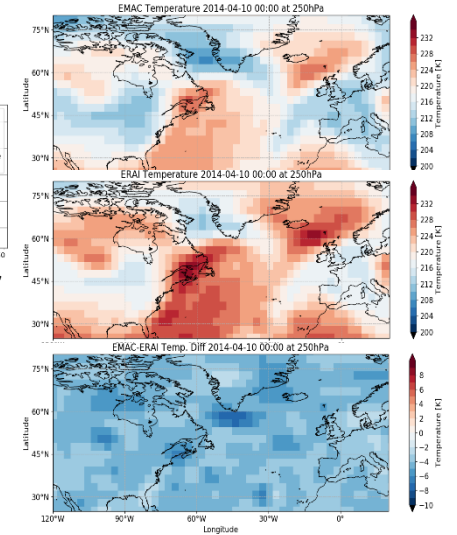
Simorg et al. 2022  
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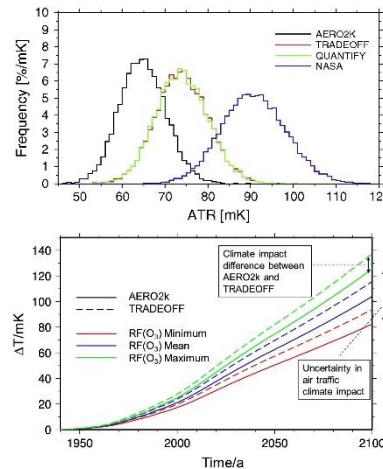


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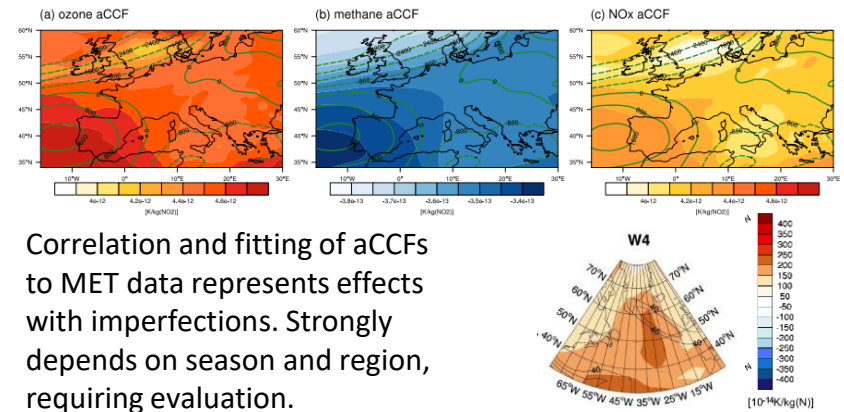
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Dahlmann et al. 2016

## Development aCCFs

### Comprehensive Lagrangian simulations in chemistry-climate



Correlation and fitting of aCCFs to MET data represents effects with imperfections. Strongly depends on season and region, requiring evaluation.

Frömming et al. 2021  
Yin et al. 2022, Dietmüller et al., 2022

# Characterization of prevailing uncertainties when providing climate change functions (CCFs)

Source of uncertainty	Origin of uncertainty
<b>Meteorological Forecast</b>	
Quality of meteorological forecast	Weather forecast data contains deviation from real world situations measured by quality of the forecast and its skill.
<b>Calculation of climate effects and impact</b>	
Representation of atmospheric processes	Chemistry scheme (e.g. O <sub>3</sub> production), cloud parametrization, horizontal and vertical resolution.
Change in GHG concentration/contrails Radiative forcing (RF)	Background (e.g. temperature bias in EMAC). Estimate of RF depends on assumption of linearity for radiative transfer calculations.
Temperature calculation	Temperature change calculation depends on assumptions on efficacy and temporal evolution of emissions/RF.
Physical climate metric	Climate metric has to be appropriate for the targeted climate objective but should still allow some variation with respect to assumptions on background emission scenario/model, emissions evolution (pulse/sustained/future scenario), climate indicator (e.g. averaged temperature response), and time horizon (e.g. ATR20).
<b>Development of Algorithms to represent CCFs (=aCCFs)</b>	
Development of algorithms in aCCFs	Due to the fitting of CCF data to meteorology at the location of emission, imperfections in the relationships are identified.
<b>Emission calculation in emission model</b>	
Emission index/conversion merged aCCFs	Assumptions in emission model.

Table from FlyATM4E: List of sources of uncertainties for individual aCCFs and for their associated calculations on climate effect.

FlyATM4E has developed a concept to **characterize prevailing uncertainties** and introduced **mathematical concepts** on how to integrate identified uncertainties in the overall climate effects assessment. This is a prerequisite in order to **characterize robustness** of alternative **climate-optimized aircraft trajectories**.

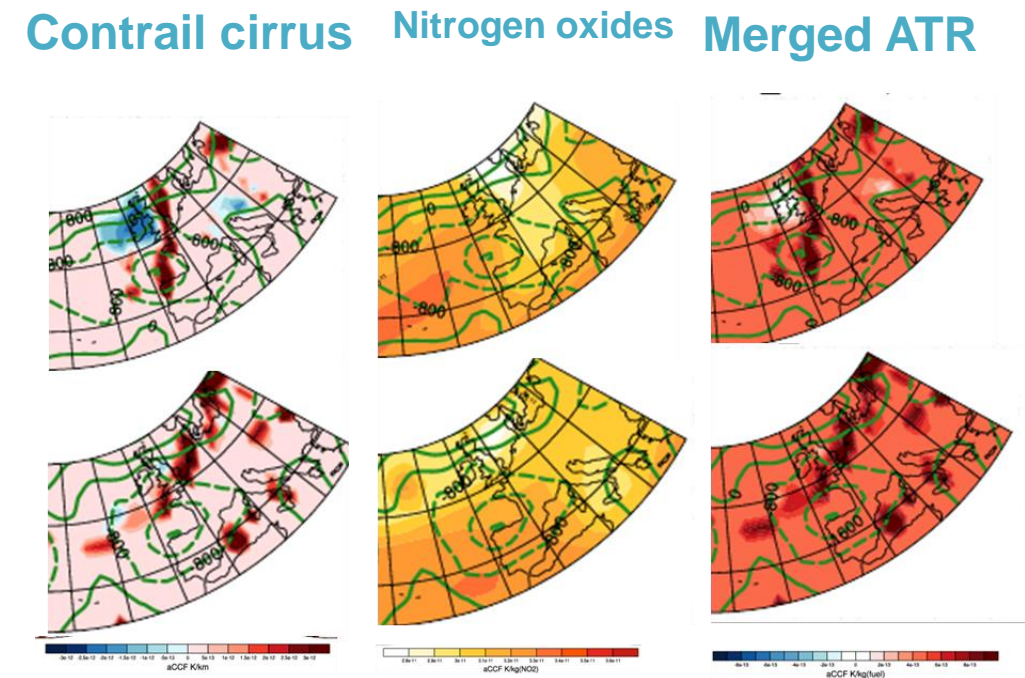
This methodology has been applied in a **case study** (summer & winter, 2018) for aircraft movements in the European Airspace where **mitigation potentials due to climate-optimized routing** have been identified (Matthes et al., 2022, *in prep.*) and their associated **uncertainty ranges** have been quantified.





## Feasibility study: Step towards robustness of climate-optimized trajectories (1/3)

- Spatial and temporal distribution of **climate effects** by climate change functions
- Expanded **environmental performance assessment** (climate metrics, sensitivity)
- **Physical climate metric**: average temperature response
- Case studies of European Air Traffic (2018) to **identify climate-optimized aircraft trajectories** quantifying total climate impact and non-CO<sub>2</sub> **mitigation potentials**.
- Two aircraft **trajectory optimization** tools (TOM, ROOST) and Earth System climate model (EMAC/DLR,TUD)
- **Cooling effects due** to contrail cirrus influences mitigation potentials



Yin et al., 2022 (in prep.)  
Dietmüller et al. 2022 (in prep)

# Feasibility study: Step towards robustness of climate-optimized trajectories (2/3)

## Implementation of prototype climate change functions

### Reanalysis data in order to identify mitigation potentials in real weather situations

Assessing weather situations and their mitigation potentials shows strong variation of climate effects with synoptic situation, season and geographic region of flight.

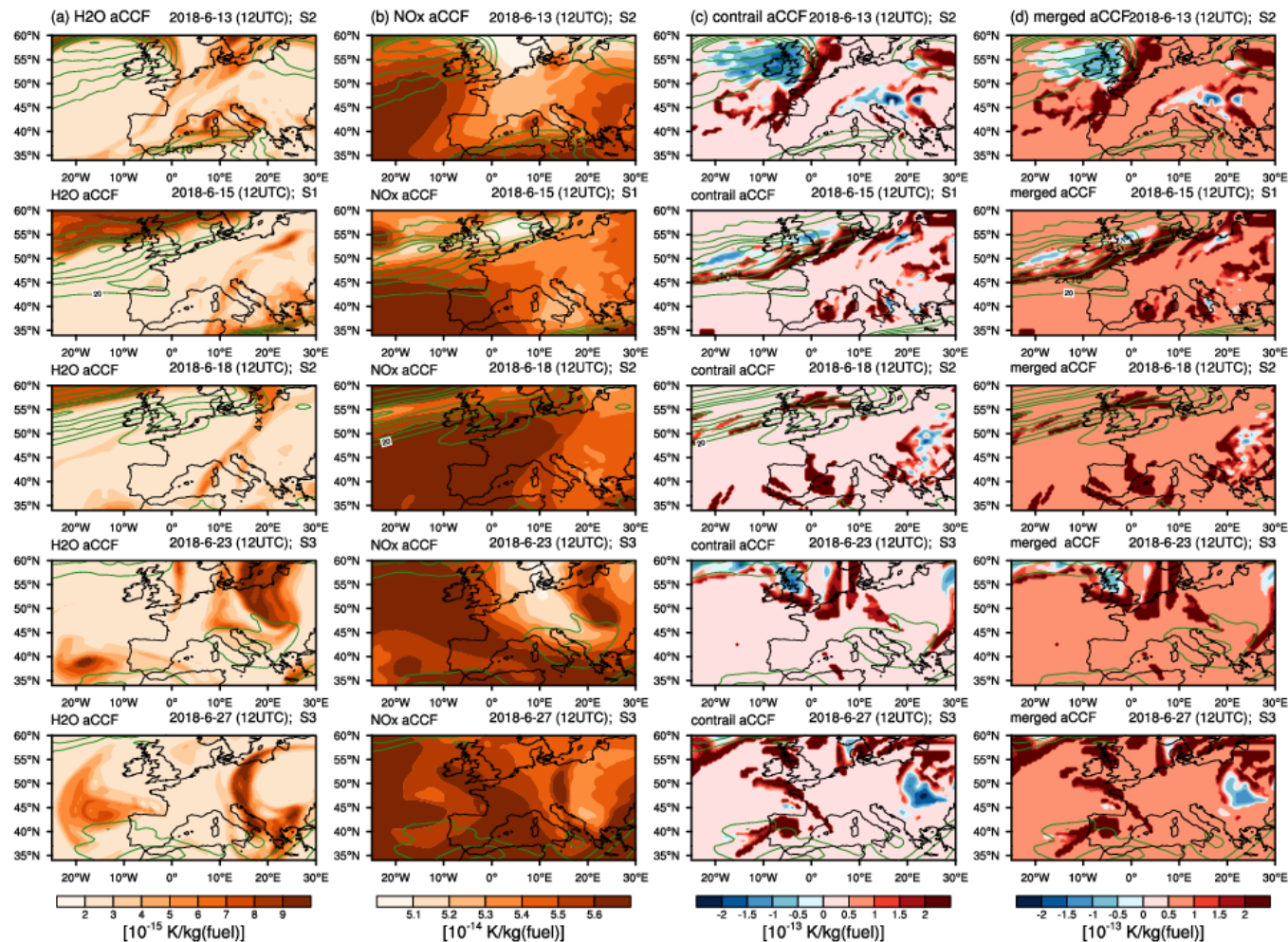
Further research is needed in order to consolidate estimates of climate effects and mitigation gains. However, feasibility studies on possible implementation are required in order to prepare for future implementation.

From earlier comprehensive climate chemistry simulations for summer and winter algorithmic climate change functions have been derived.

Applying these algorithms to reanalysis data allows to quantify anticipated climate effect for a given geographic position and time of flight.

Climate metrics (ATR) were calculated with climate response model AirClim

Individual non-CO<sub>2</sub> climate effects show different type of granularity, strength and temporal variation of regions with high impact.



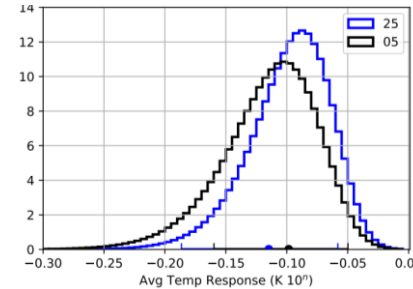
Matthes et al. 2022



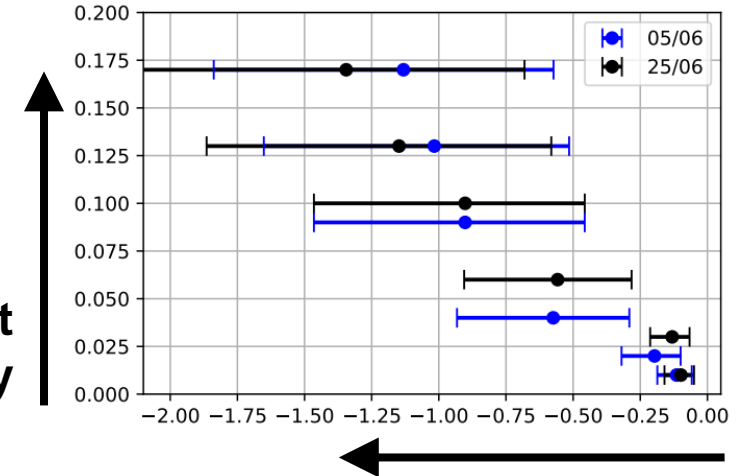
# Feasibility study: Step towards robustness of climate-optimized trajectories (3/3)

- Pareto front of optimized solutions
- Mitigation potential & Uncertainty depends on synoptic situation.
- Monte-Carlo risks assessment to assess robustness of identified mitigation options
- Strategies for efficient solutions from a system approach rely on marginal costs

## Uncertainty analysis (normal & lognormal)



Cost penalty



## NO<sub>x</sub> effects of European Air Traffic (Jan-Dec)



Matthes et al. 2022

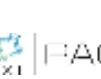
- Beyond two offline trajectory optimizers the Earth System Climate model **EMAC/AirTraf** is used for optimization
- Pareto principle confirms that e.g. 20% of the flights contribute about 80% of the reduction
- Strong seasonal dependence of mitigation potentials can be characterized leading to optimization strategies

Castino et al. 2021



This project has received funding from the SESAR Joint Undertaking under grant agreements No 699395 and No 891317 under European Union's Horizon 2020 research and innovation programme.

# D-KULT: LuFo Projekt (2022-2025)



## Zielsetzung

### • Nachweis der Machbarkeit ökoeffizienter Flugtrajektorien

- im europäischen Luftraum (größere Möglichkeit zur Reduzierung der Klimawirkung, laterale Abweichungen leichter möglich, aber mehr Einrichtungen involviert),
- im deutschen Luftraum (potentiell mehr Zwangsbedingungen durch Start und Landung, leichtere reale Umsetzbarkeit durch einheitliche nationale Zuständigkeit).

## Technische Ziele

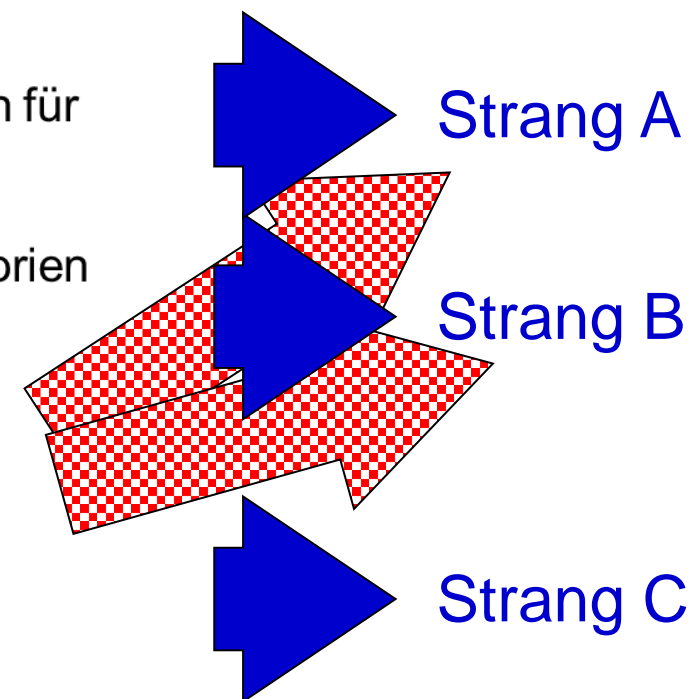
- Die Bildung von persistenten Kondensstreifen und Kondensstreifen-Zirren für realen Luftverkehr vermeiden.
- Ein Flugplanungssystem für klima-freundliche (öko-effiziente) Flugtrajektorien auf der Basis von algorithmische Klimawirkungsfunktionen (aCCC) implementieren.
- Die Machbarkeit von klima-freundliche Flugtrajektorien demonstrieren.
- Methoden für lärmarmen An- und Abflug unter Berücksichtigung der Klimawirksamkeit weiterentwickeln.



# D-KULT: LuFo Projekt (2022-2025)

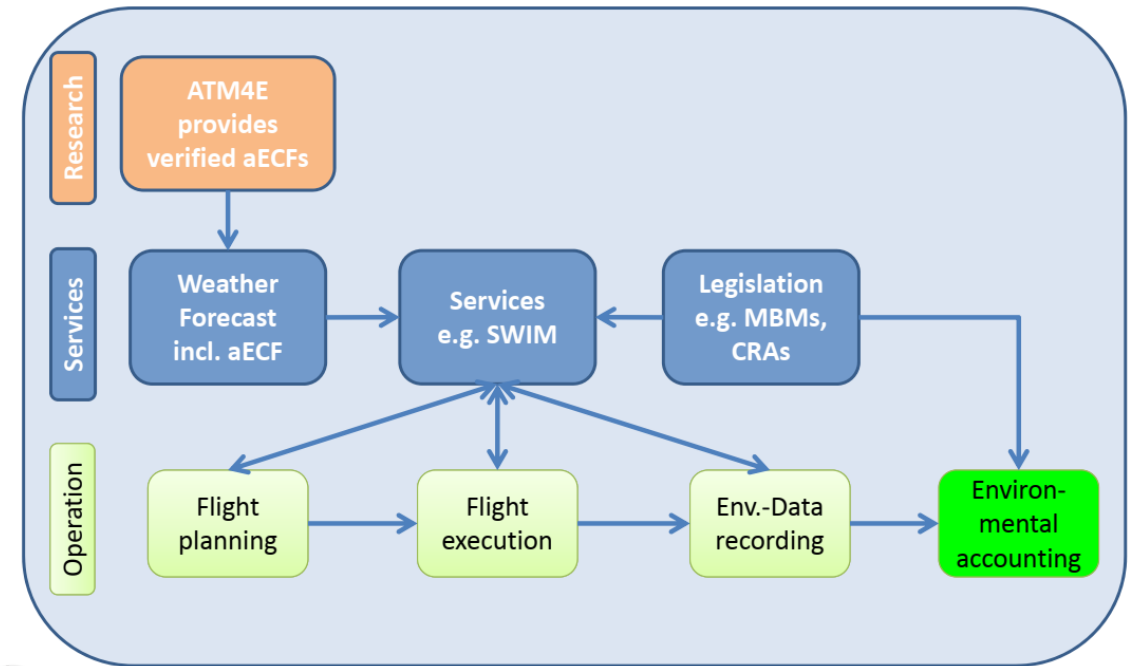
## Umsetzung

- Die Bildung von persistenten Kondensstreifen und Kondensstreifen-Zirren für realen Luftverkehr vermeiden.
- Ein Flugplanungssystem für klima-freundliche (öko-effiziente) Flugtrajektorien auf der Basis von algorithmische Klimawirkungsfunktionen (aCCC) implementieren.
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## Roadmap: Towards implementation of climate-optimized trajectories

- Implementation relies on **provision of climate change functions to ATM** (trajectory optimisation)
- Feasibility study performed on **infrastructure** comprising MET components – resulting in roadmap definition how to expand the current ATM system in order to **enable climate-optimized trajectories**
- Options on how to **develop and how to integrate such novel MET products** have been studied in earlier projects, e.g. DG Aeronautics (**REACT4C**, 2010-2013) and SESAR2020 (e.g. **ATM4E**, 2016-2018).
- Candidate solutions are proposed: enabling solution relying on aCCFs (**Sol-FlyATM4E-01**) and operational solution on climate optimized trajectories (**Sol-FlyATM4E-01**)
- Further options on how to expand current ATM and how to identify overall **mitigation potential by climate-optimized trajectories** are currently explored, e.g. ongoing SESAR2020 (Exploratory Research) FlyATM4E, ALARM, but also Aeronautics ClimOP and ACACIA.
- Concepts on how to deal with **prevailing uncertainties** are required for a **robust decision making**.



Matthes et al. 2017



# Danke für Ihre Aufmerksamkeit

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# Literature and references

<https://flyatm4e.eu/>

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